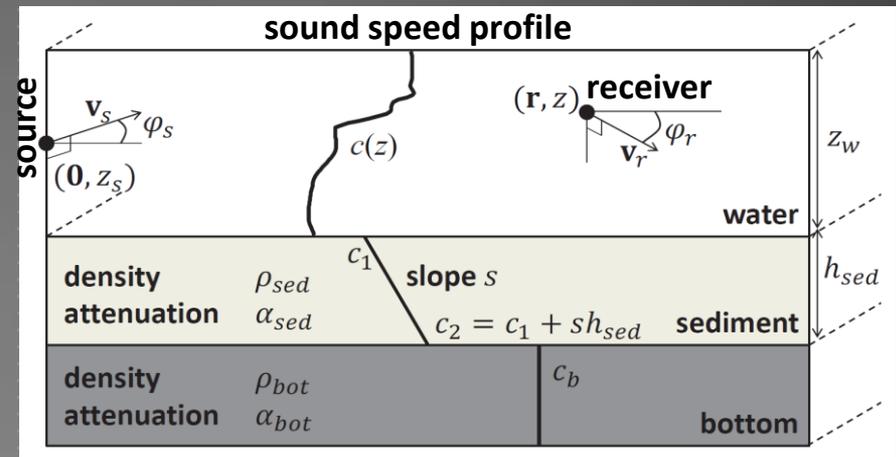


# SYNTHETIC APERTURE GEOACOUSTIC INVERSION IN THE PRESENCE OF RADIAL VELOCITY AND ACCELERATION DYNAMICS

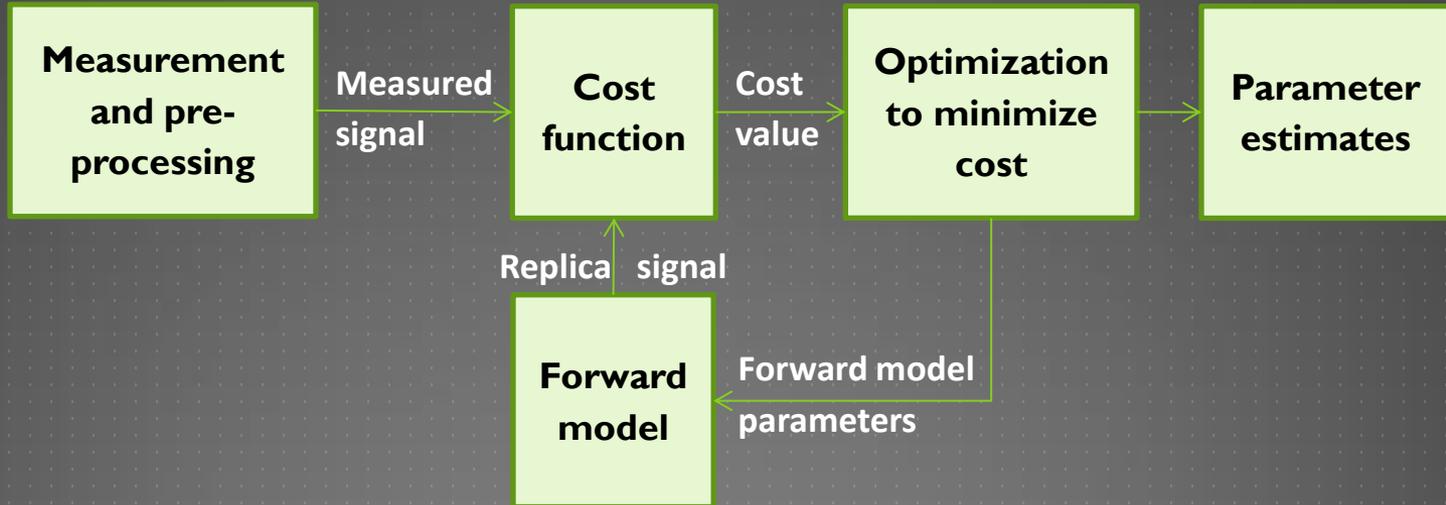
Bien Aik Tan, Peter Gerstoft, Caglar Yardim and William Hodgkiss

- ❑ Mobile single source and receiver matched field inversion method for low SNR
- ❑ Long observation time of P LFM chirps
- ❑ Requires waveguide Doppler
- ❑ Constant radial velocity constraint
- ❑ Extension to acceleration

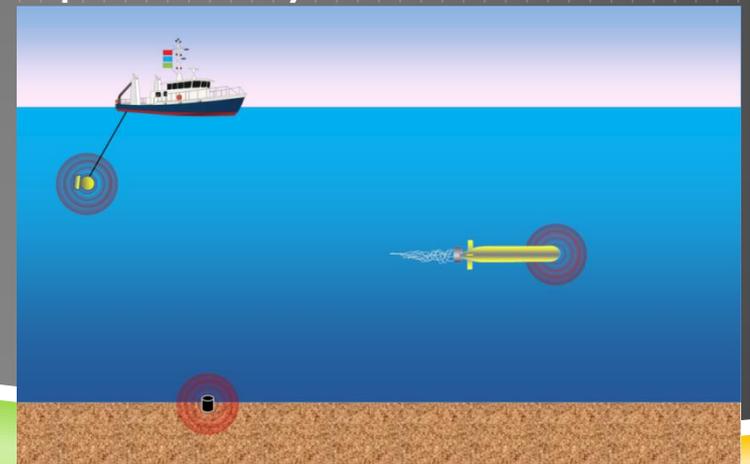
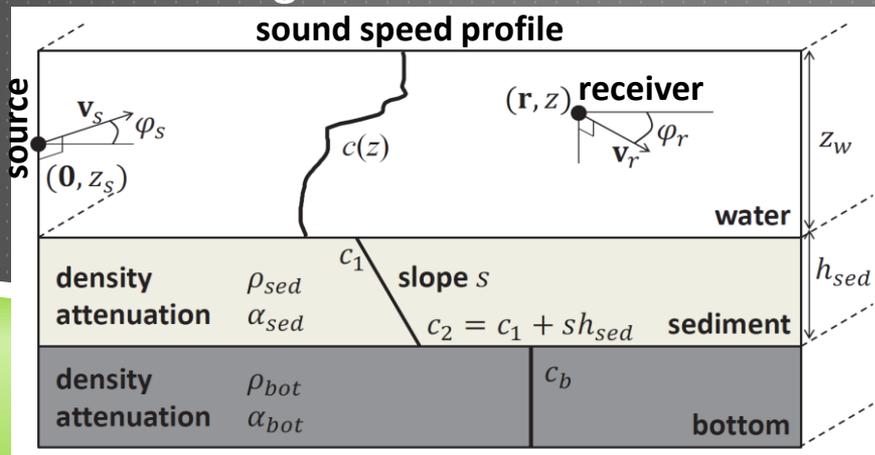


# BACKGROUND / MOTIVATION

## ► Generic inversion process



## ► Mobile single source/receiver method – operationally attractive



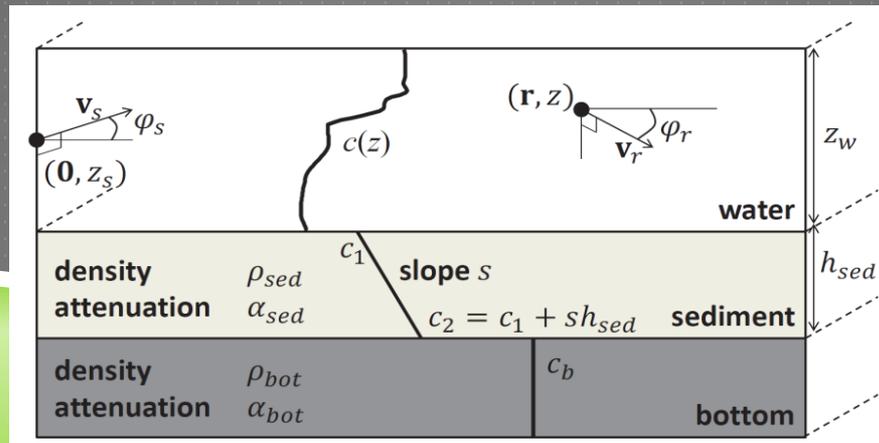
# MOTIVATION

- ▶ Low SNR / source power
  - ▶ Most methods works on the basis of high SNR/source power
  - ▶ Concern for disturbance of marine mammals (Gervaise 2012)
  - ▶ Development of expendable/low powered acoustic sources for AUV based survey (Massa) (source level restrictions, rapid environment assessment by AUV)
- ▶ Existing single source/receiver methods
  - ▶ Modal dispersion curve analysis (Bonnell, Gervaise)
  - ▶ Matched impulse response method (Josso, Le Gac, Jesus, Hursky, Hermand)
  - ▶ Matched field processing method (Siderius, Tan)
  - ▶ Synthetic aperture modal inverse method (Frisk, Rajan)



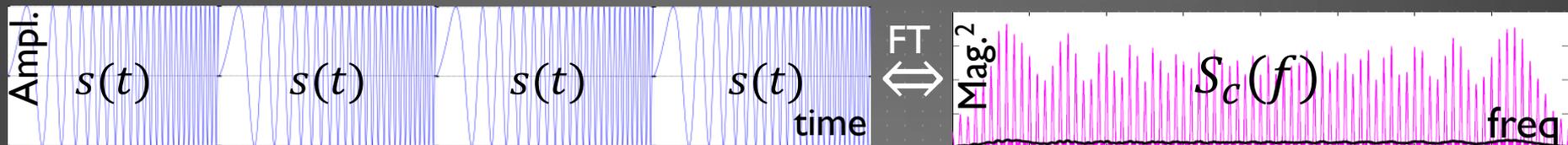
# PREVIOUS WORK

- ▶ **Tan et al, “Broadband synthetic aperture geoacoustic inversion”, JASA, 2013.**
  - ❑ Mobile single source and receiver method for low SNR
  - ❑ Lost of spatial diversity and array gain (w.r.t to VLA)
  - ❑ Broadband frequency coherent method (100-900 Hz)
  - ❑ Long observation time (64 s) of P LFM chirps (1 s)
  - ❑ But method becomes Doppler/motion intolerant., requires waveguide Doppler model
  - ❑ **Assume constant horizontal source/receiver radial velocities**



# COHERENTLY EXPLOITING MULTIPLE LFMS

- ▶ P LFMs
- ▶ 100–900 Hz  $T=1$  s  $T_r=1$  s
- ▶ Periodic peaks at  $1/T_r$  Hz
- ▶ Peak samplings and doubling P
  - ▶ Signal peak increases 6 dB
  - ▶ Noise level increase 3 dB
  - ▶  $6 - 3 = 3$  dB gain
  - ▶ Increasingly Doppler intolerant

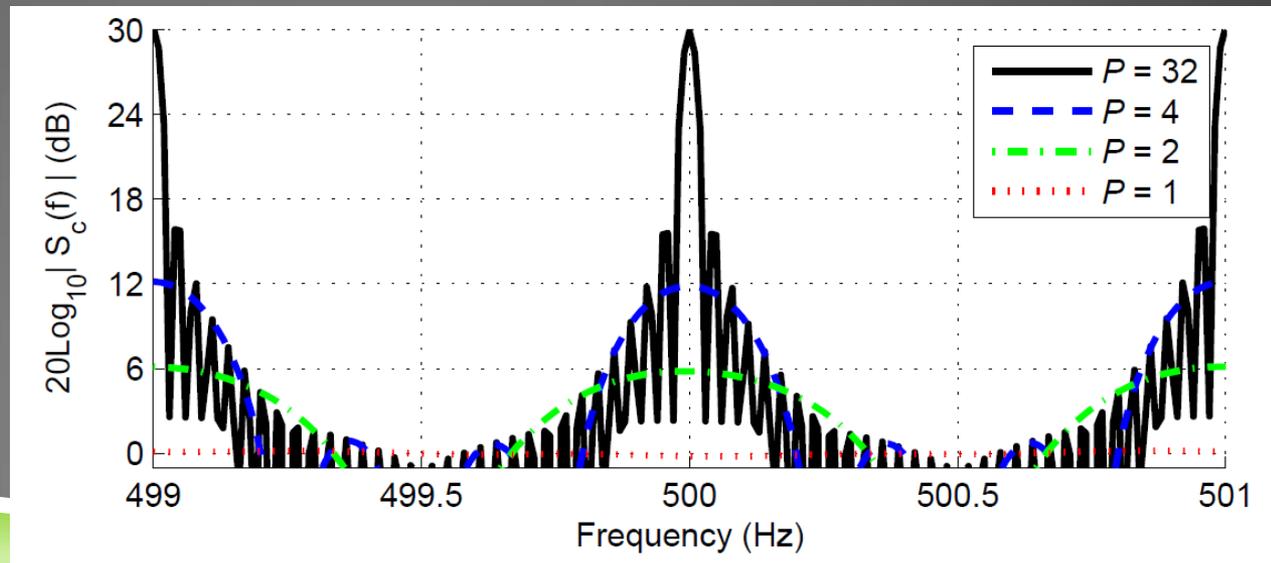


$$S_c(f) = \sum_{p=0}^{P-1} \exp(i2\pi f p T_r) S(f)$$

$$\{S(t) * \sum \delta(t - nT_r)\} \times \text{rect}\left\{\frac{t - PT_r/2}{PT_r}\right\}$$

↕ FT

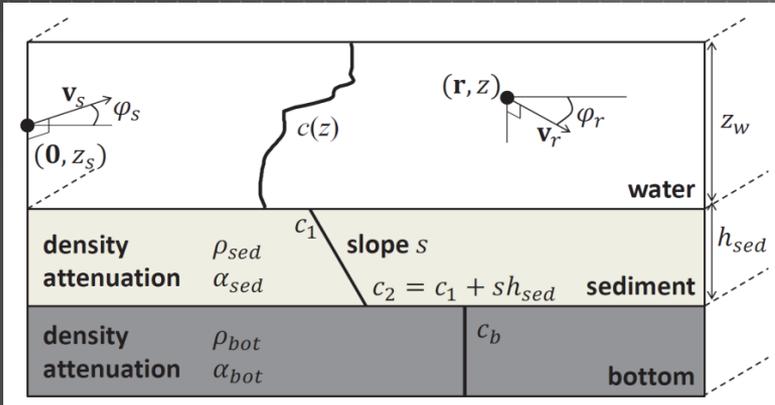
$$\{S(f) \times \sum \delta(f - j/T_r)\} * PT_r \text{sinc}\{fPT_r\}$$



# WAVEGUIDE DOPPLER

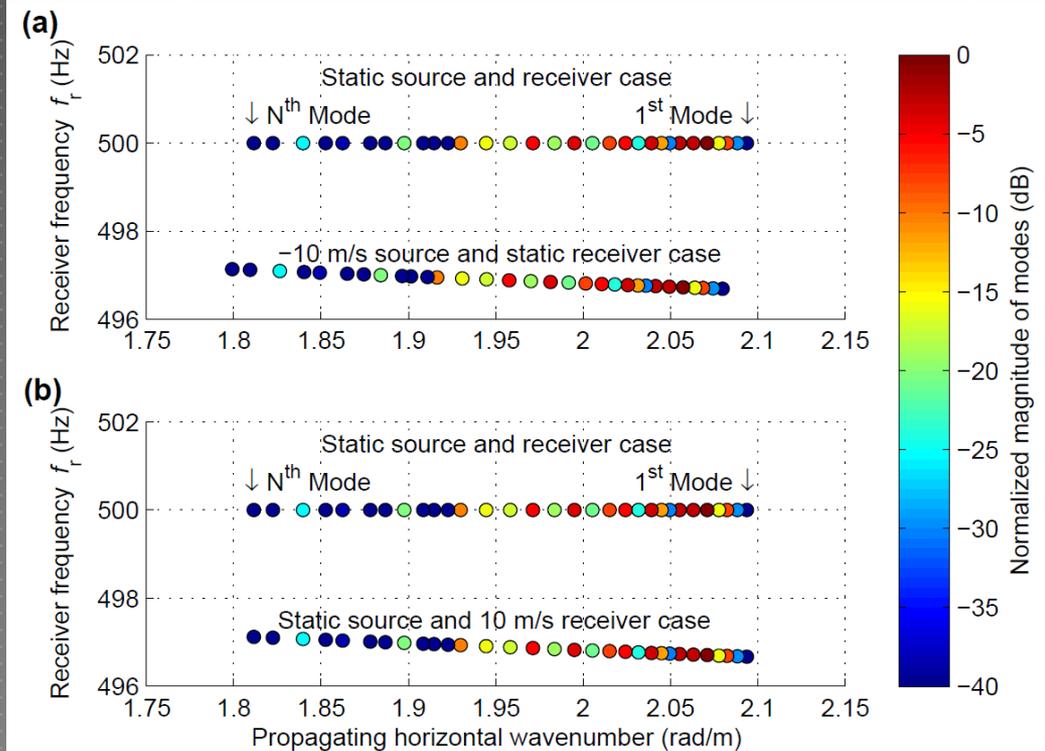
## ► 1994 Schmidt and Kuperman

- Spectral/**Modal** Solution
- Non-reciprocity
- Frequency domain



- Each mode has a different Doppler

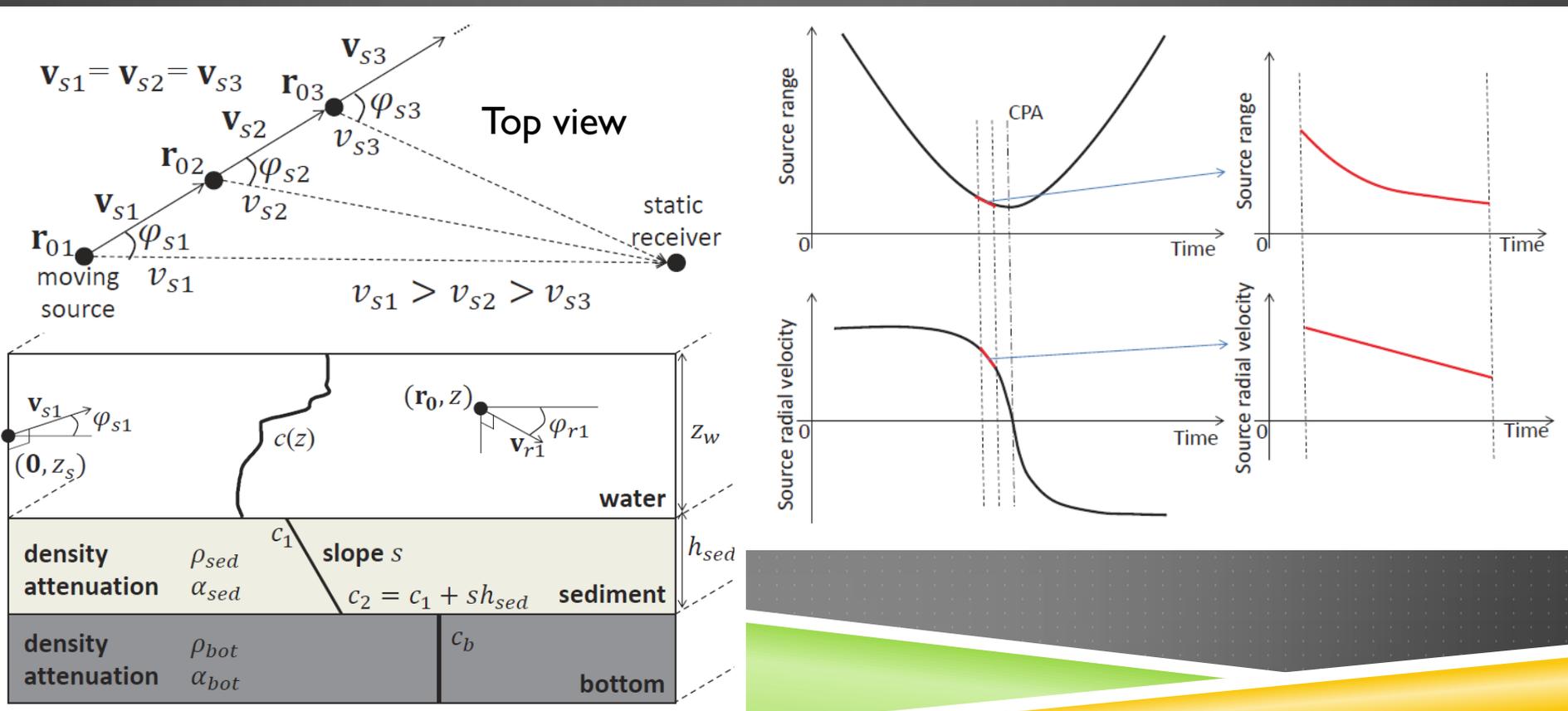
Example: 500 Hz harmonic source (KRAKEN)



Source	Propagation	Receiver
$\omega_s^{(k_n)} = \omega_r - k_n(v_s - v_r)$	$\omega = \omega_r + k_n v_r$	$\omega_r$
$\omega_s$	$\omega = \omega_s + k_n v_s$	$\omega_r^{(k_n)} = \omega_s + k_n(v_s - v_r)$

# FOR THIS OCEANS PAPER...

- ▶ Extend previous method to more practical scenarios such as near CPA or when radial velocity changes.
- ▶ Allow pulse dependent changes in source/receiver radial velocities



# COMPUTE $\psi(\mathbf{r}, z, \omega_r)$

Source	Propagation	Receiver
$\omega_s^{(k_{np})} = \omega_r - k_{np}(v_{sp} - v_{rp})$	$\omega = \omega_r + k_{np}v_{rp}$	$\omega_r$
$\omega_s$	$\omega = \omega_s + k_{np}v_{sp}$	$\omega_r^{(k_{np})} = \omega_s + k_{np}(v_{sp} - v_{rp})$

- ▶ However, modeling acceleration is non-trivial
- ▶ Time varying modal wavenumbers and functions (Walker 2007)
- ▶ Circumvent by approximating acceleration
- ▶ Assume radial velocities are piece-wise constant for each pulse
- ▶ But radial velocities are linearly changing pulse to pulse

Compute normal modes (normalized) as per static case  $\{\Psi_n(z_s), \Psi_n(z), k_{rn}, u_{rn}\} @ \omega_r$

For each pulse, assume  $\{v_{s1}, v_{r1}, p, a_s, a_r\}$  known. Compute the propagation horizontal wave number  $k_{np}$

Extract the source spectrum  $S(\omega_r - k_{np}(v_{sp} - v_{rp}))$  and coherently combine all pulses to give  $\psi(\mathbf{r}, z, \omega_r)$

# COMPUTE $\psi(\mathbf{r}_0, z, \omega_r)$

Source	Propagation	Receiver
$\omega_s^{(k_{np})} = \omega_r - k_{np}(v_{sp} - v_{rp})$	$\omega = \omega_r + k_{np}v_{rp}$	$\omega_r$
$\omega_s$	$\omega = \omega_s + k_{np}v_{sp}$	$\omega_r^{(k_{np})} = \omega_s + k_{np}(v_{sp} - v_{rp})$

- ▶  $\psi(\mathbf{r}, z, \omega_r) \approx \frac{ie^{-i\frac{\pi}{4}}}{\sqrt{8\pi\rho(z_s)}} \sum_p \exp(i\omega_r(p-1)T_r) \sum_n S(\omega_r - k_{np}(v_{sp} - v_{rp})) \Psi_n(z_s; \omega_r) \Psi_n(z; \omega_r) \frac{e^{ik_{np}r_{op}}}{\sqrt{k_{np}r_{op}}}$
- ▶ where  $k_{np} \approx \frac{k_{rn}}{\left(1 - \frac{v_{rp}}{u_{rn}}\right)} \approx \frac{k_{sn}}{\left(1 - \frac{v_{sp}}{u_{sn}}\right)}$  is the mode and pulse dependent propagating wavenumber and for any arbitrary  $\omega_r$  or  $\omega_s$
- ▶  $v_{sp} = v_{s1} + (p-1)T_r a_s$  and  $v_{rp} = v_{r1} + (p-1)T_r a_r$

Compute normal modes (normalized) as per static case  $\{\Psi_n(z_s), \Psi_n(z), k_{rn}, u_{rn}\}$  @  $\omega_r$

For each pulse, assume  $\{v_{s1}, v_{r1}, p, a_s, a_r\}$  known. Compute the propagation horizontal wave number  $k_{np}$

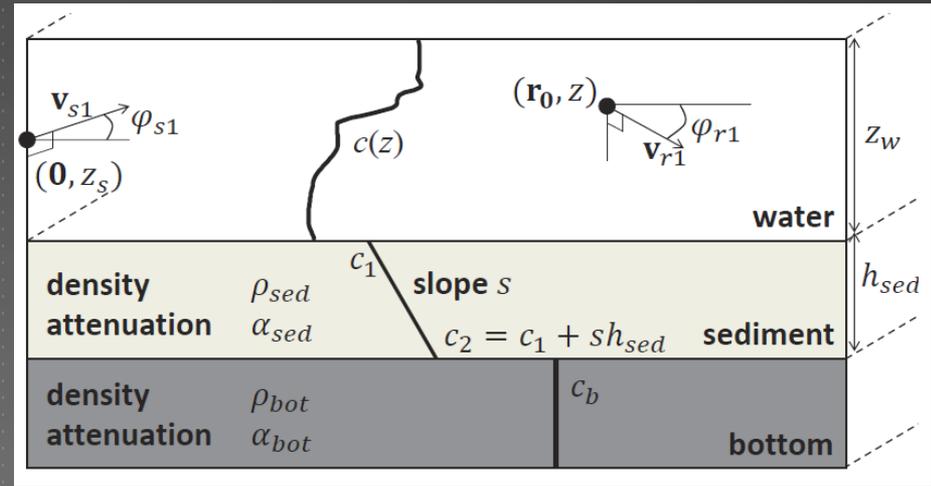
Extract the source spectrum  $S(\omega_r - k_{np}(v_{sp} - v_{rp}))$  and coherently combine all pulses to give  $\psi(\mathbf{r}, z, \omega_r)$

# SW06 SIMULATION

LFM 100–900 Hz  $T=1$  s  $T_r=1$  s

- ▶ Moving source & static receiver
  - ▶ Coherently exploit P=64 LFM
- ▶ Source initial radial vel. 1.9 m/s
- ▶ Source acceleration -0.006 m/s<sup>2</sup>
- ▶ Source depth 30 m
- ▶ Receiver depth 45 m
- ▶ Source range at t = 0,  $r_0=600$  m
- ▶ SNR = 0 dB
- ▶ Sampling interval  $\Delta f=5$  Hz

GA

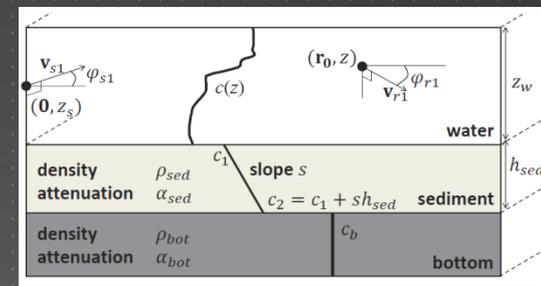


$$\begin{aligned} \{\xi, \mathbf{x}\}_{ML} &= \arg \max_{\xi, \mathbf{x}} \left[ \ln L(\xi, \mathbf{x}) \right] \\ &= \arg \min_{\xi, \mathbf{x}} \left[ 10 \log_{10} \Phi(\xi, \mathbf{x}) \right] \end{aligned}$$

where the cost function

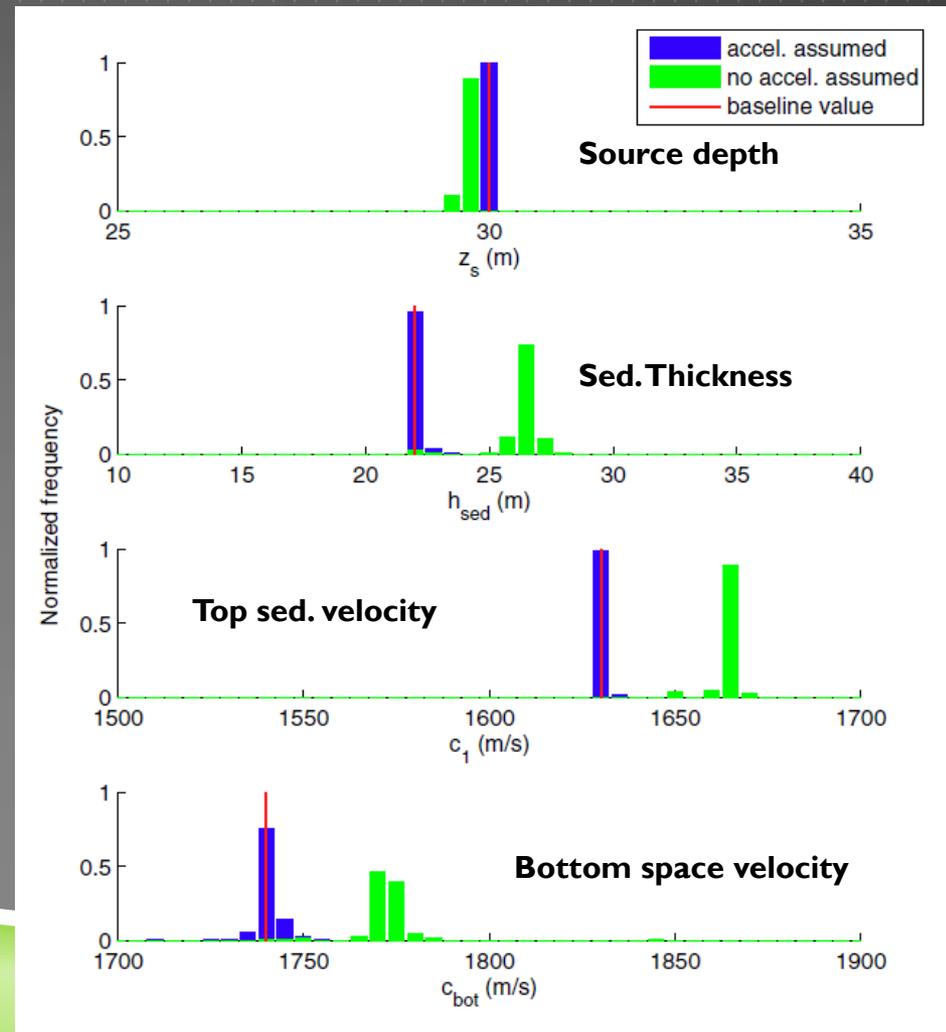
$$\Phi(\xi, \mathbf{x}) = 1 - \frac{|\mathbf{y}^H \tilde{\mathbf{C}}_w^{-1} \mathbf{b}|^2}{\mathbf{y}^H \tilde{\mathbf{C}}_w^{-1} \mathbf{y} \mathbf{b}^H \tilde{\mathbf{C}}_w^{-1} \mathbf{b}}$$

# MOVING SOURCE & STATIC RECEIVER



Monte Carlo inversion  $P = 64$

- ❑ 200 noise realizations
- ❑ SNR = 0 dB
- ❑ Executed twice
  - ❑ Forward model include acceleration (Blue)
  - ❑ Forward model assumes no acceleration (Green)



# SW06 EXPERIMENT

- ▶ JD238 2040 UTC
- ▶ Source: J-15, 30 m, LFM 100–900 Hz  $T=1$  s  $T_r=1$  s,
- ▶ Receiver: Hydrophone 8 of VLA, 44.6 m
- ▶ Source – receiver range ~600m
- ▶ Initial radial velocity ~1.6 m/s with acceleration ~ -0.006 m/s<sup>2</sup> SNR ~ 0 dB

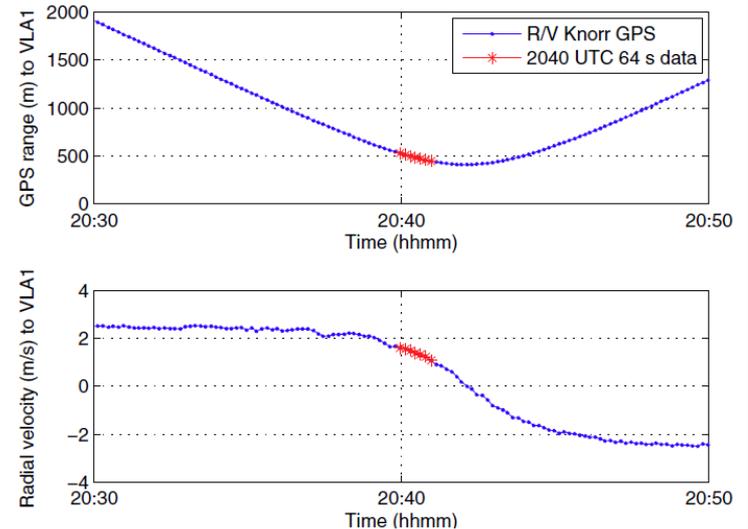
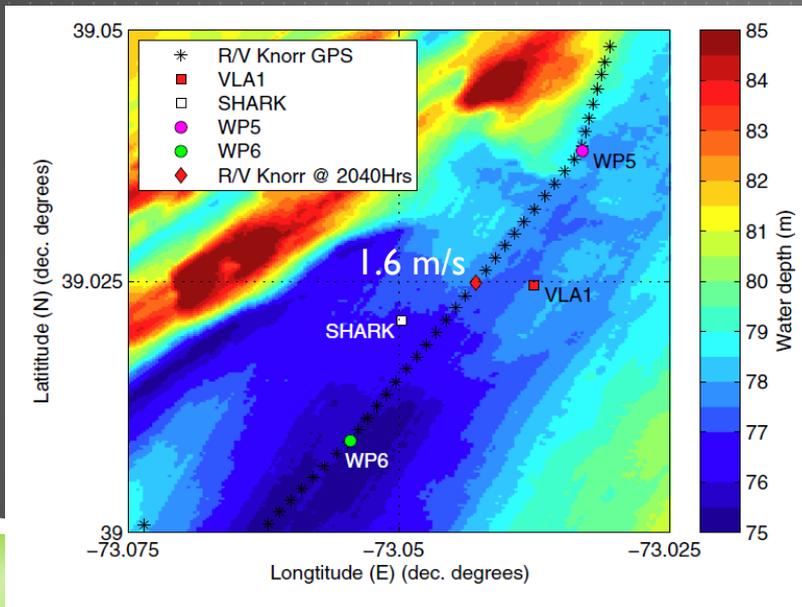
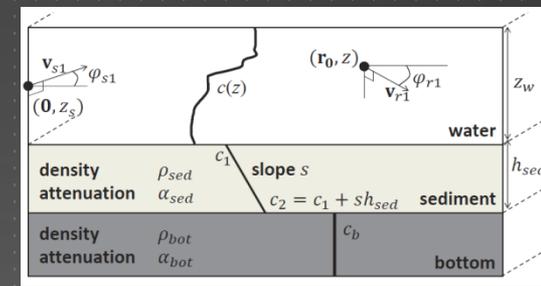
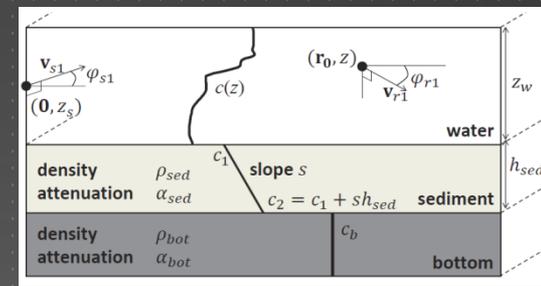


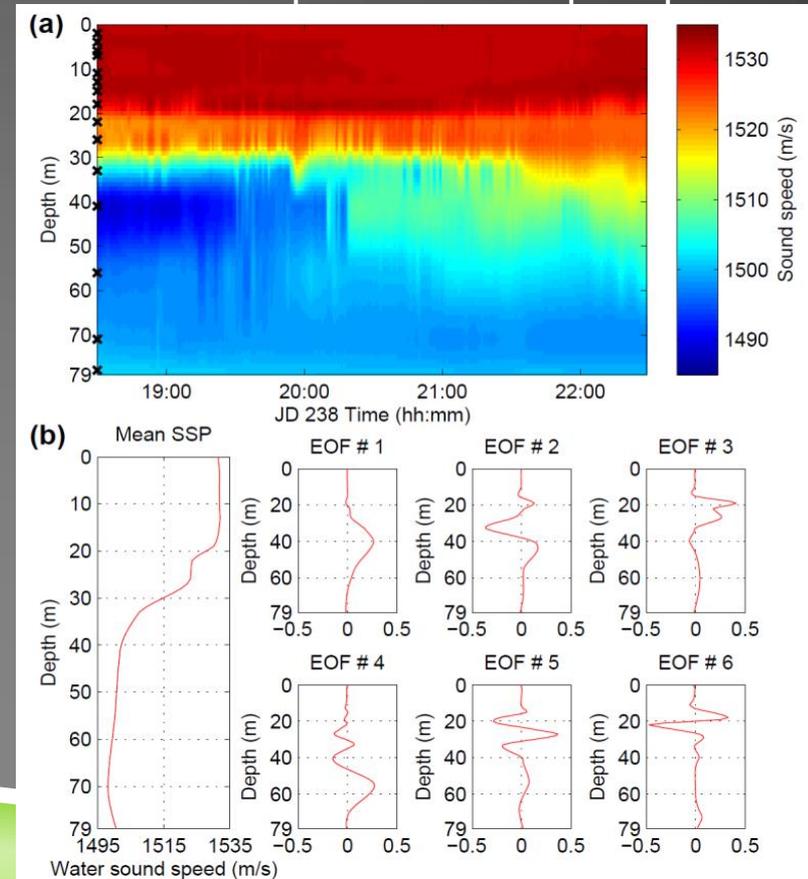
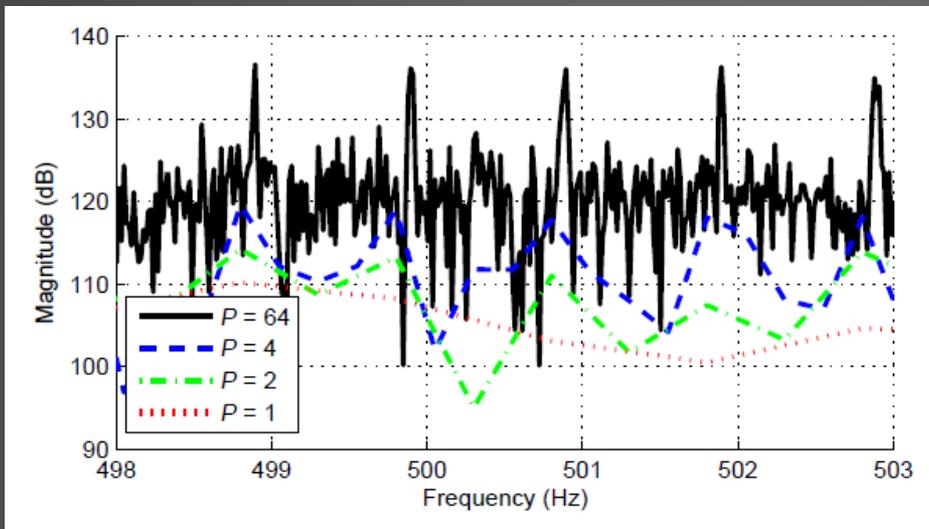
Fig. 7. R/V Knorr Telemetry

# SW06 RECEIVED SPECTRUM AND EOFs

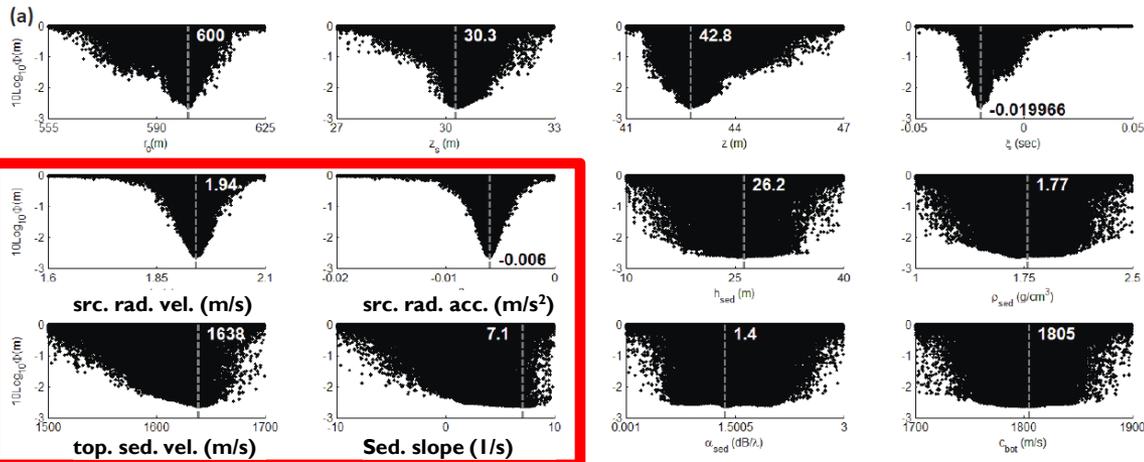


- ▶ Section of SW06 received signal spectrum with LFM pulses  $P = [1, 2, 4, 64]$

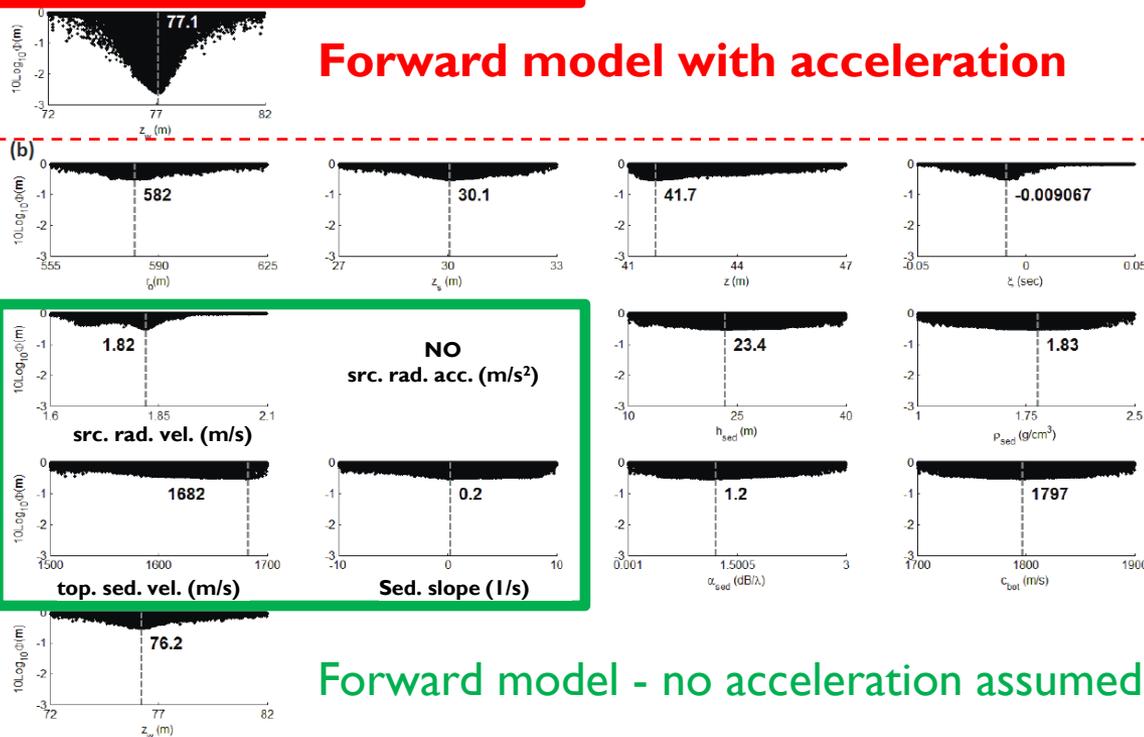
SHARK interpolated sound speed profile



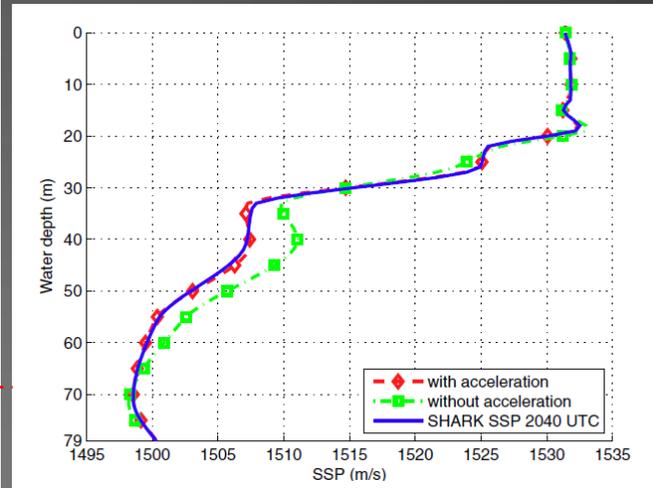
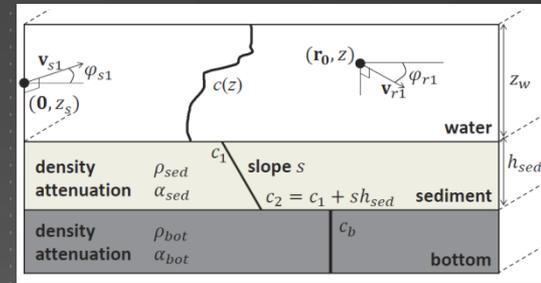
# INVERSION RESULTS P=64



**Forward model with acceleration**



**Forward model - no acceleration assumed**



- Sediment velocity profile estimate adversely affected
- Relatively lower sensitivities = higher estimation uncertainties

- ❑ Extends broadband synthetic aperture geoacoustic inversion to cases where radial velocities change.
- ❑ Well-suited for horizontally accelerated source/receiver.
- ❑ Demonstrated in simulation/real data that modeling **radial** acceleration is critical for correct inversion

# CONCLUSIONS

Discussions...

Questions and answers...

Acknowledgements:



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